

# Raking Echoes in the Time-Domain

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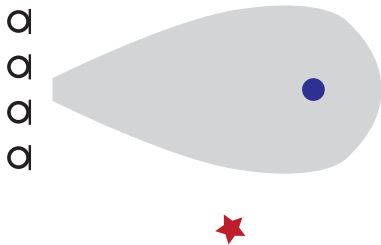
Tuesday Afternoon Meeting  
April 1, 2015

Echoes are good!

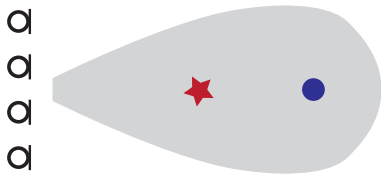
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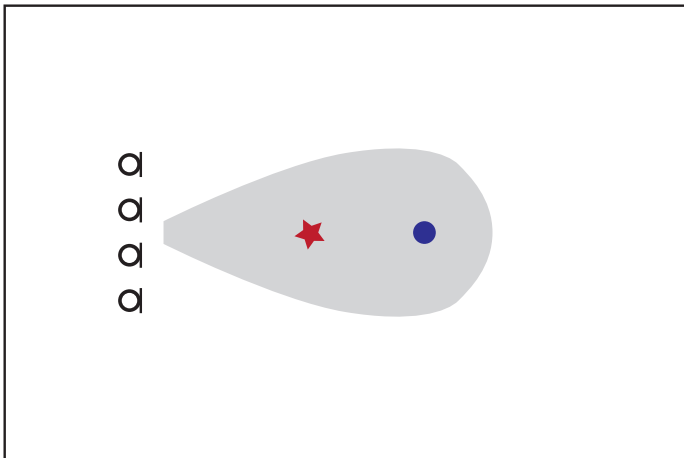


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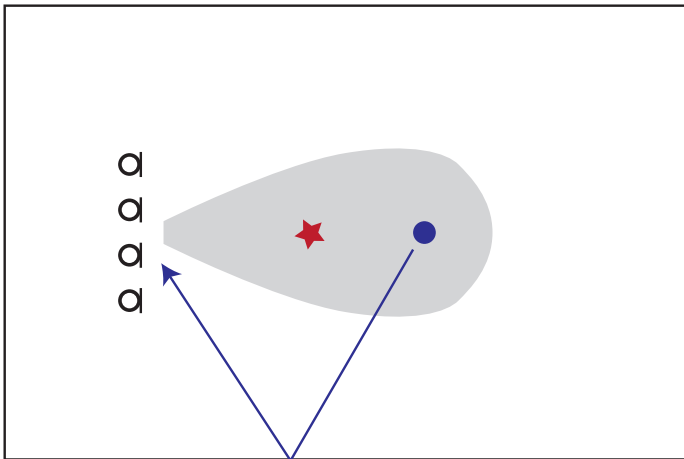




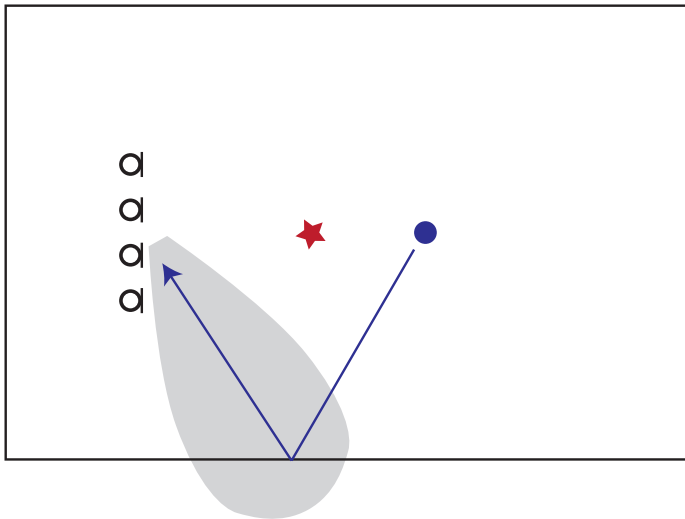
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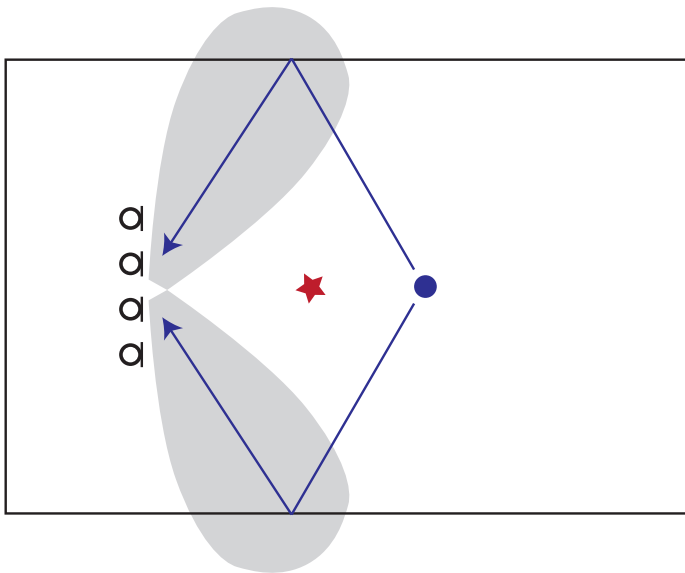
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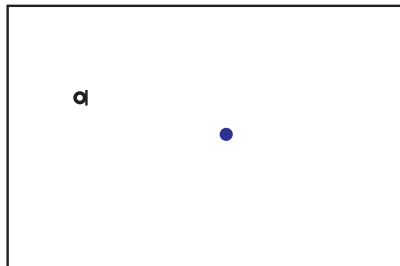
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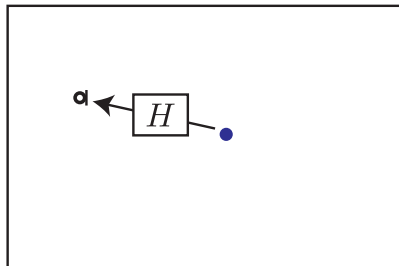


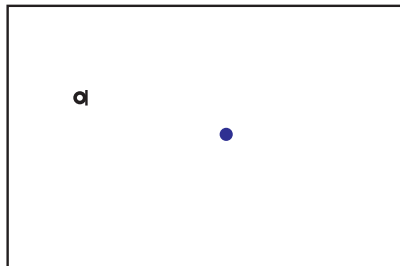
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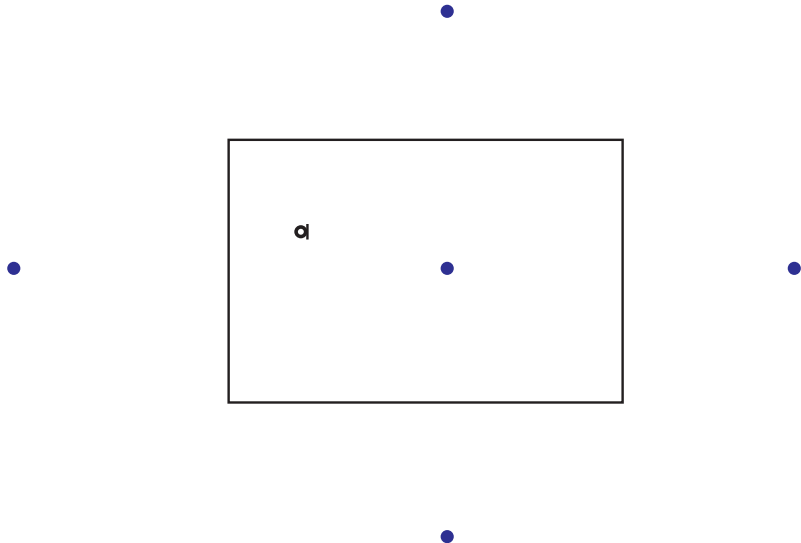
1. Model and notation
2. Raking beamformers
3. Results

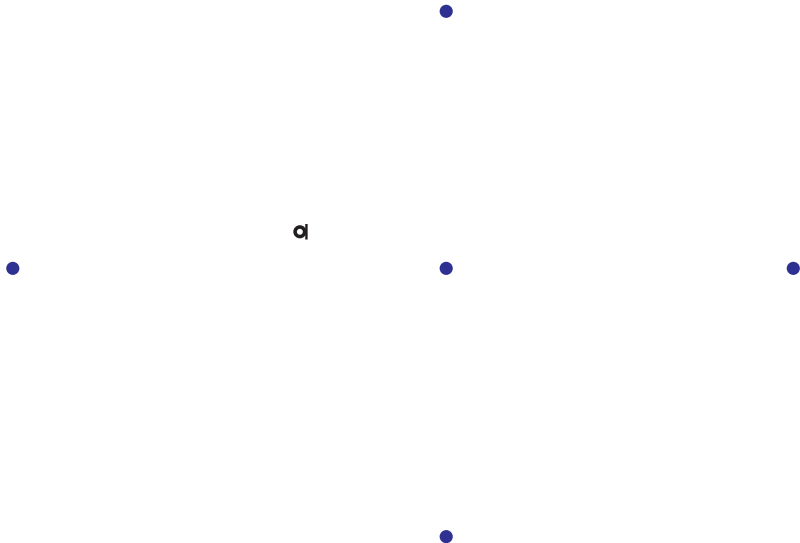


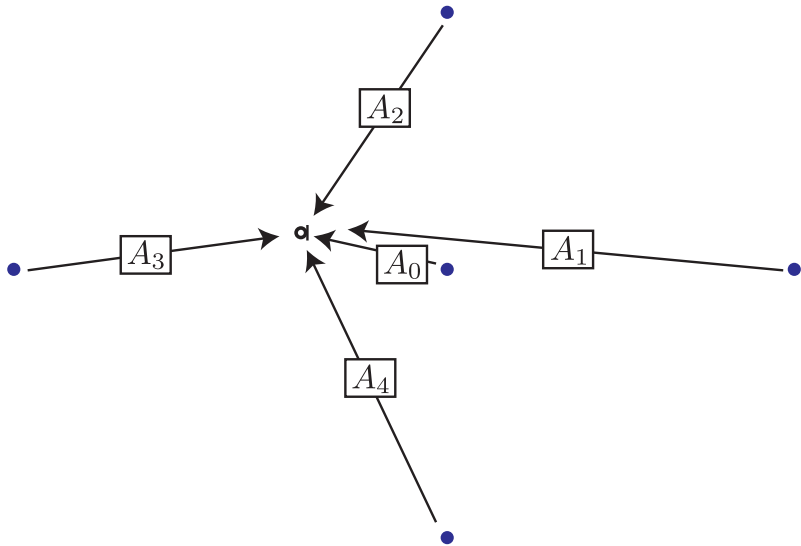












Mic 1

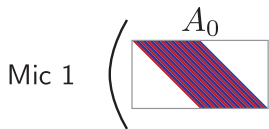
Source signal



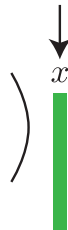
$x$



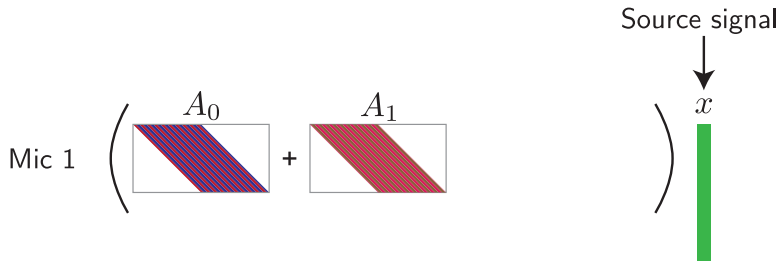
# Compact notation

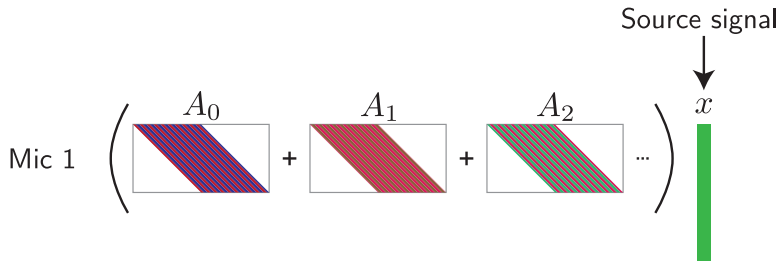


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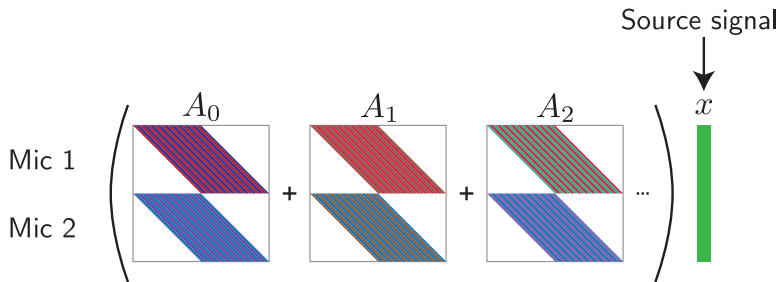


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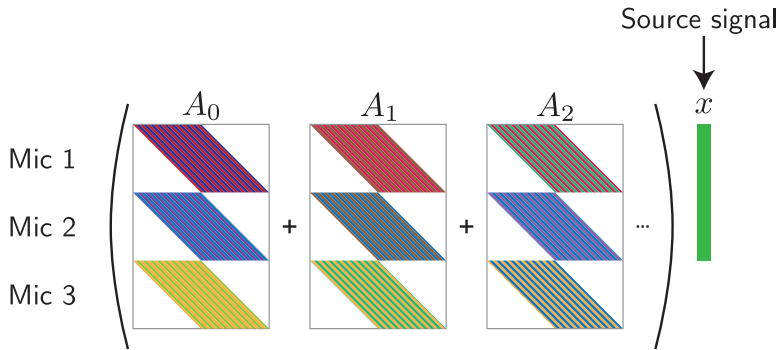


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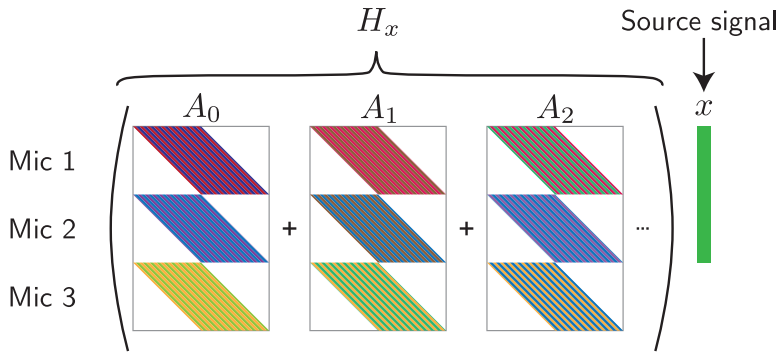




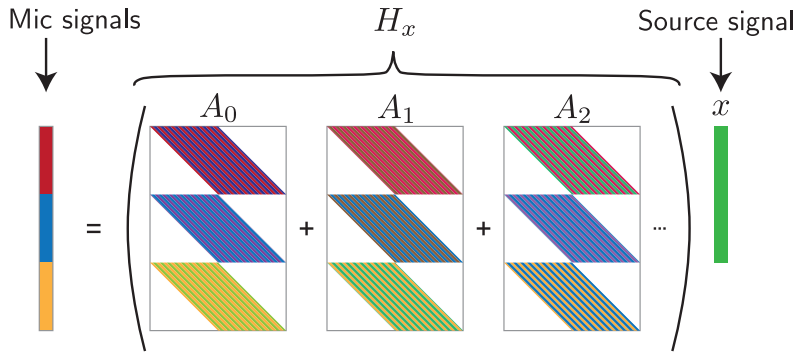
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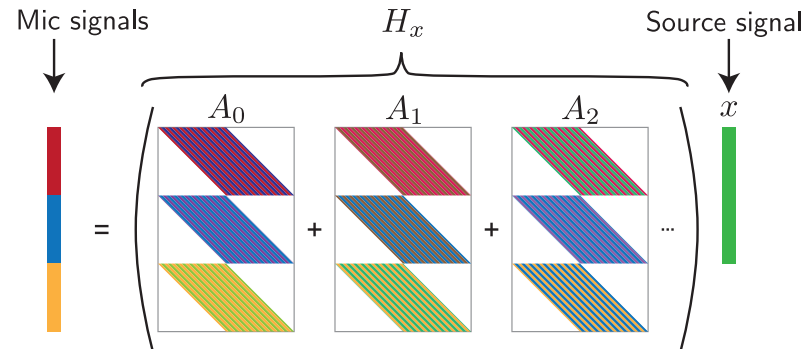


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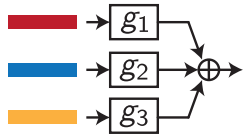


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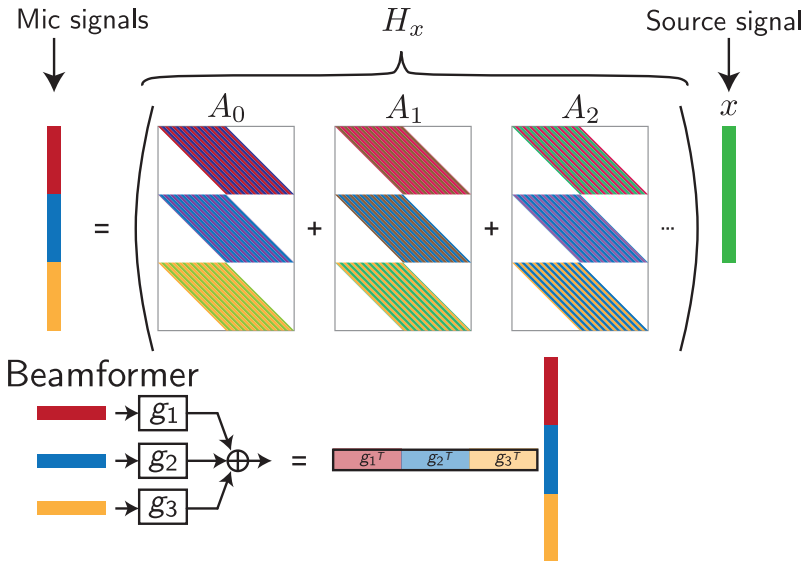




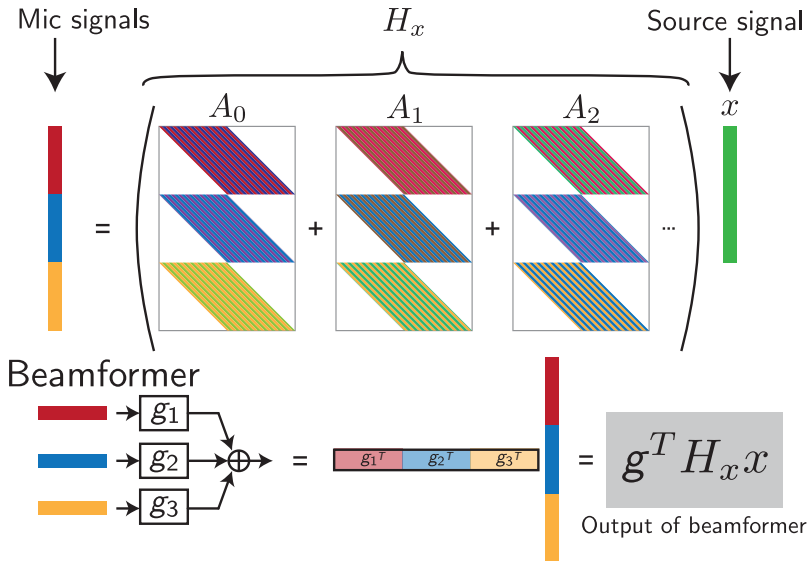
Beamformer

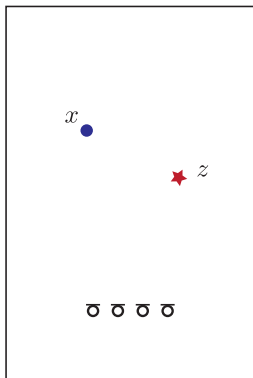


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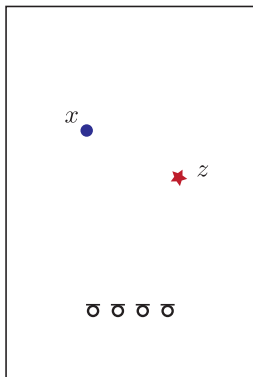


- Signal model:

$$y = H_x x + H_z z + n$$

- $H_x$  and  $H_z$  constructed from geometry
- Beamformer response

$$u_x = H_x^T g \quad u_z = H_z^T g$$



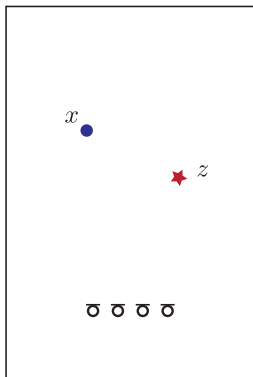
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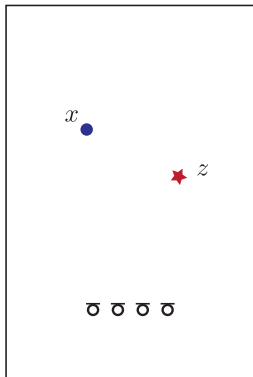


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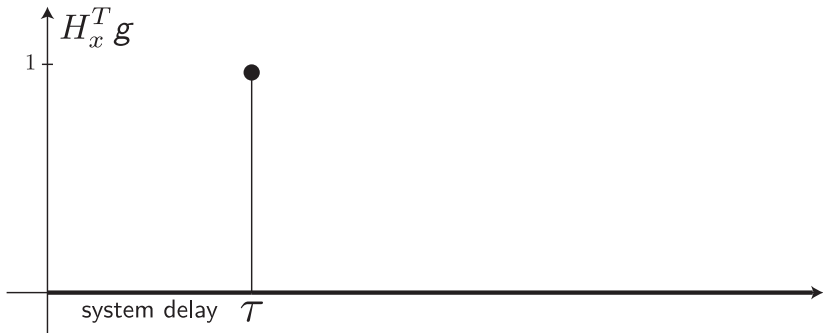
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# Minimum variance distortionless response beamformer

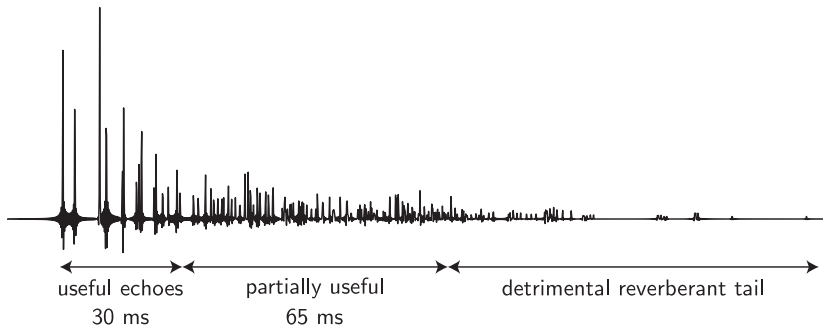
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# Clues from perceptual acoustics



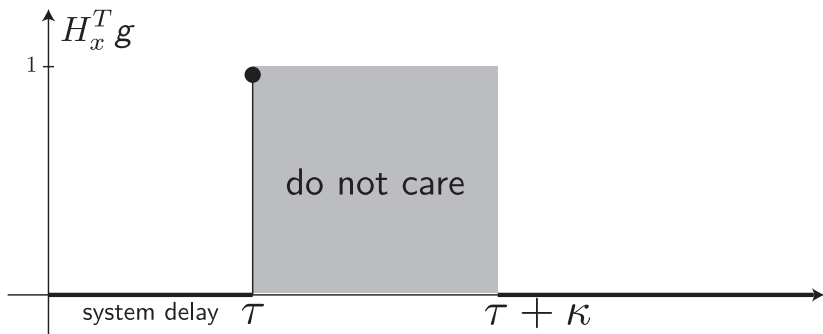
J. Lochner, J.F. Burger, *The Influence of Reflections on Auditorium Acoustics*, 1964.

## Relaxing the distortionless constraint

$$\underset{\mathbf{g}}{\text{minimize}} \mathbb{E} \|\mathbf{g}^T (\mathbf{H}_z \mathbf{z} + \mathbf{n})\|^2 \quad \text{subject to } \mathcal{M} \mathbf{H}_x^T \mathbf{g} = \delta_\tau$$

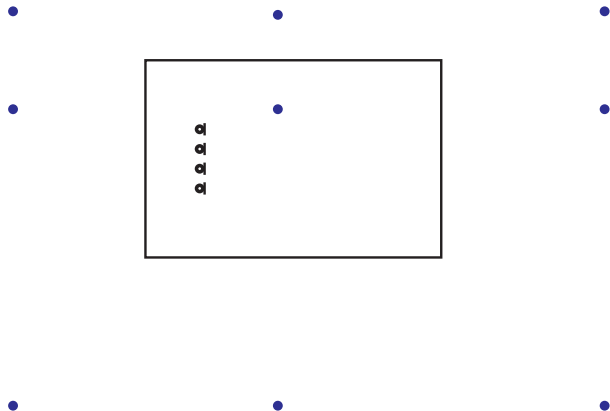
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# Image source picking

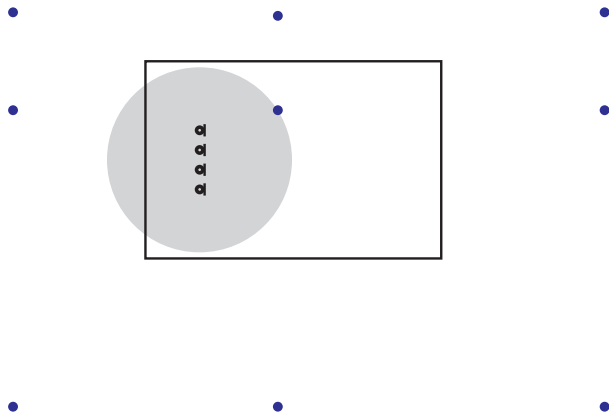
- MVDR: Sources within  $c\tau$  contribute energy
- Perceptual: Sources within  $c(\tau + \kappa)$  contribute energy



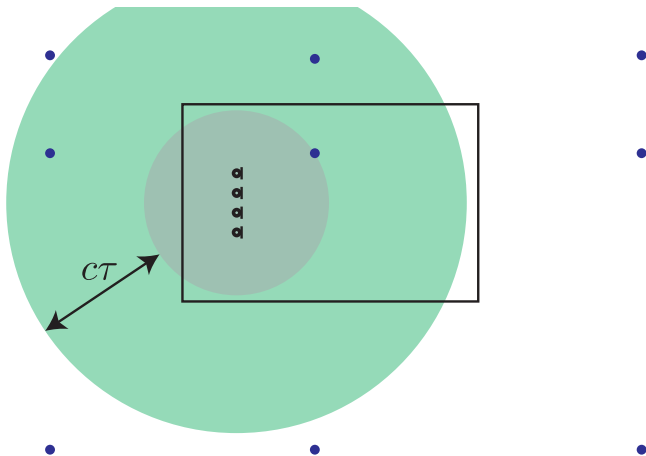


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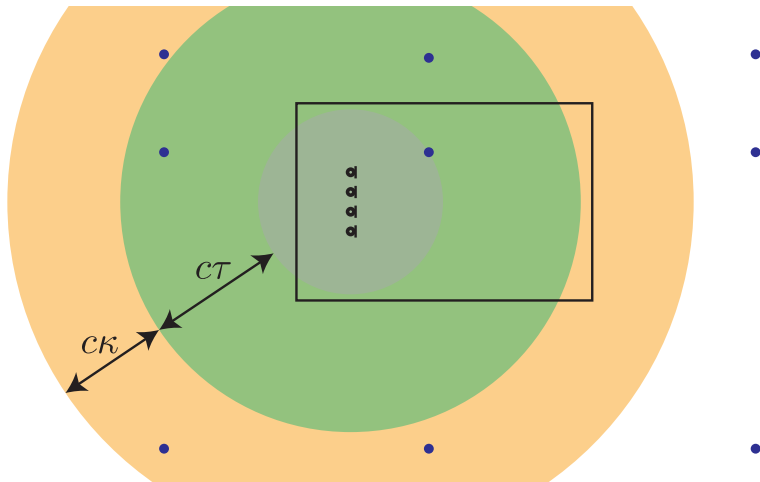


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- Performance metric:

$$\text{SINR} = \mathbb{E} \left[ \frac{\|\mathbf{g}^T \mathbf{H}_x \mathbf{x}\|^2}{\|\mathbf{g}^T (\mathbf{H}_z \mathbf{z} + \mathbf{n})\|^2} \right]$$

- Optimal beamformer:

maximize<sub>*g*</sub> SINR

- Response very distorted : not practical
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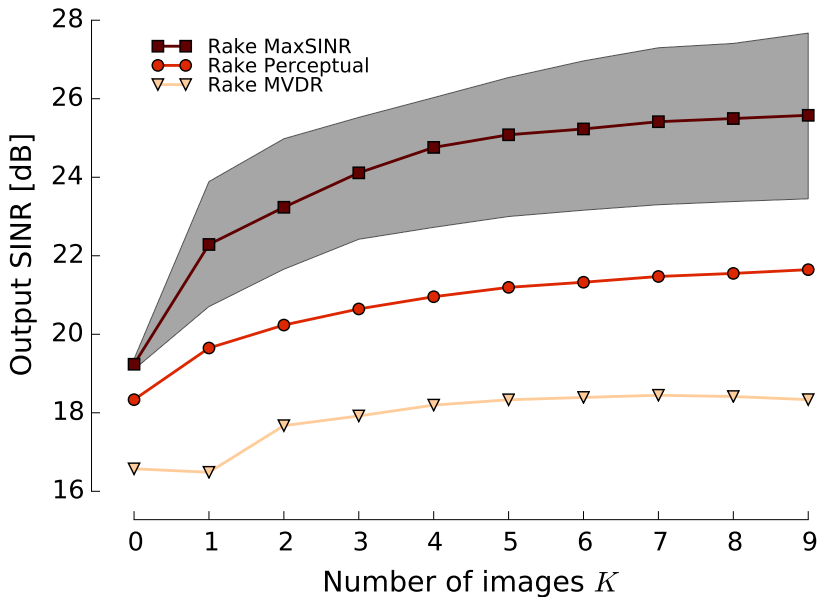
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# SINR improvements





## Contribution

- A distortionless raking beamformer
- A perceptually motivated raking beamformer
- Time-domain designs allow control on:
  - Delay
  - Pre-echoes
- SINR increases with number of image sources
- Python framework

## What's next ?

- Robust formulations
- Experiments

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# Thanks for your attention!



Code and figures available at  
[http://lcav.github.io/  
TimeDomainAcousticRakeReceiver/](http://lcav.github.io/TimeDomainAcousticRakeReceiver/)